Using Auctions as Coordination Mechanisms for Planning Perishable Crop Production

A. Nicholas Mason, J. Rene Villalobos Ph.D., Hector Flores

Arizona State University

School of Computing, Informatics and Decision Systems Engineering July 2014

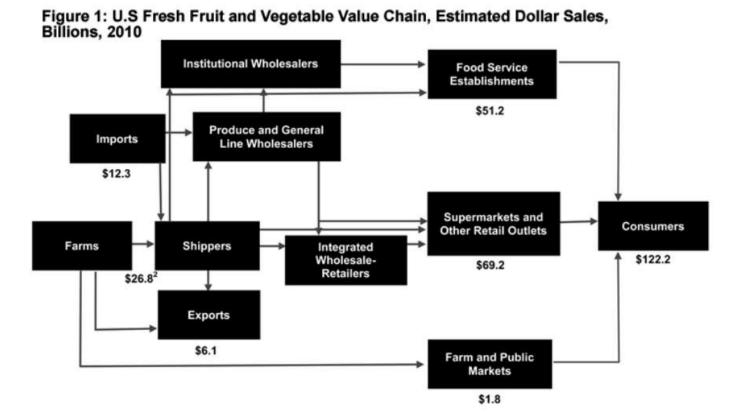
Agenda:

- Problem background and motivation
- Description of the problem
- Literature review
- Solution approach
- Mathematical model
- Numerical results
- Further considerations



Background:

 Consolidation in the industry is changing the balance of power to the detriment of producers who lag far behind (U.S. Case)



Background:

Producer Impact Concerns:

 Long lead times, yield/price variability, weather uncertainty, retailer requirements and short shelf lives

Environmental Concerns:

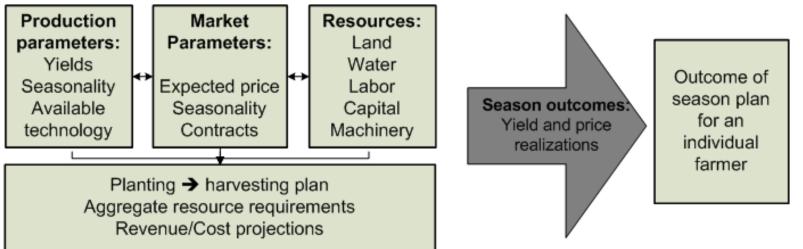
- Food consumption is set to double by 2050
- Current levels of food waste are significant
 - Over 50% for fruits and vegetables
 - 30% lost before reaching the consumer

Producers are responding by **forming cooperatives** and **joint consolidation centers**



Farmers:

- Make critical tactical decisions which will influence their entire season
- Must account for many relevant variables, both certain and uncertain





Planting Periods

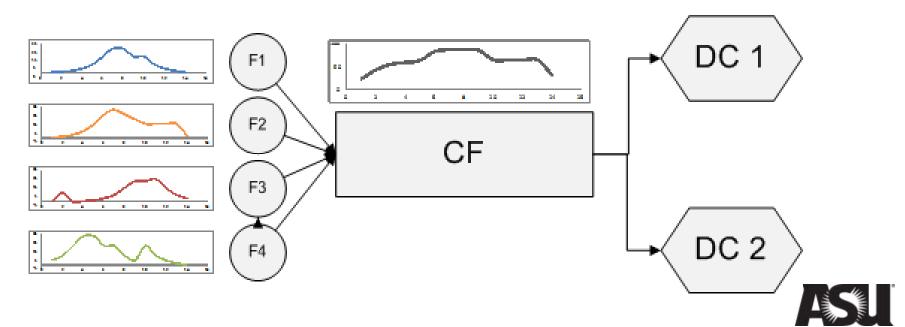
Harvesting Periods



																На	arve	st b	y w	/eek														
		N	love	mb	er	D)ece	emb	er		Jan	uary	/		Febr	ruar	у		Ма	arch			Ap	oril			M	ay			Ju	ne		
Date of Plant	Production	1	2	3	4	1	2	3	4	1	2	3	4	1	2	3	4	1	2	3	4	1	2	3	4	1	2	3	4	1	2	3	4	· %
15-Aug	1,662			5	5	10	10	10	10	9	9	8	8	8	8																			100
30-Aug	1,828					5	5	10	10	10	10	9	9	8	8	8	8																	100
14-Sep	2,373					5	5	6	10	10	10	10	10	9	9	8	8																	100
29-Sep	2,564							5	5	10	10	10	10	9	9	8	8	8	8															100
14-Oct	2,698									5	5	10	10	10	10	9	9	8	8	8	8													100
29-Oct	2,684											5	5	10	10	10	10	9	9	8	8	8	8											100
13-Nov	2,896													5	5	10	10	10	10	9	9	8	8	8	8									100
28-Nov	2,837															5	5	10	10	10	10	9	9	8	8	8	8							100
13-Dec	2,337															5	5	10	10	10	10	9	9	8	8	8	8							100
28-Dec	2,183																	5	6	10	20	22	10	8	7	6	6							100
12-Jan	1,794																			4	5	10	15	22	10	9	9	8	8					100
27-Jan	1,385																					7	7	13	13	18	18	9	9	4	2			100
11-Feb	1,200																					7	7	21	21	15	15	5	4	3	2	1	5	在0
26-Feb	948																							6	6	16	17	12	12	8	8	ĥ	1,1	E.O

Consolidation Facility:

- Role of CF is to pool variance of production, achieve economies of scale and allow year-round availability of products
- Entry point to the cold-chain

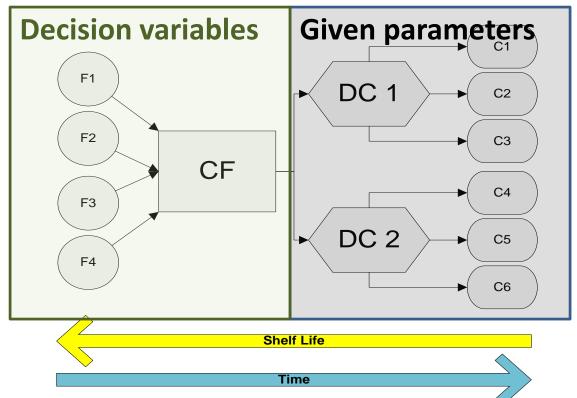


We seek to **coordinate the supply chain** such that **optimal** production and marketing decisions are made **as if** they were taken by **a single, centralized, decision maker**

Must create the right incentives, decision support technologies and collaboration frameworks



- First echelon of the supply chain
 - Producers and consolidation points
- Tactical decisions





Key Problem Considerations:

- There should be transparency and fairness on contract allocation
- Agents may act strategically and attempt to influence allocation decisions
- Incentive Compatibility: No agent can be made better off by misrepresenting its information
- Individual Rationality: Agents cannot be forced to participate



Related literature:

Mechanism design and auctions:

- Auctions for price discovery and efficient allocation (Vickrey, 1961)
- Efficiency of auctions (Myerson, 1981)
- Auction mechanisms have been proposed as viable tools to achieve coordination (Vohra, 2011)
- For horizontal coordination, *a marriage between auction mechanisms and supply contracts* may be promising (Chen, 2003)



Related literature:

Supply chain coordination:

- Multiple proposals for SC coordinating auctions have been proposed (Karabuk & Wu, 2002; Fan, Stallaert, & Whinston, 2003; Mishra & Veeramani, 2007)
 - Few account for incentive compatibility
 - None exist for agriculture (in particular, for fresh produce)

Agricultural supply chains:

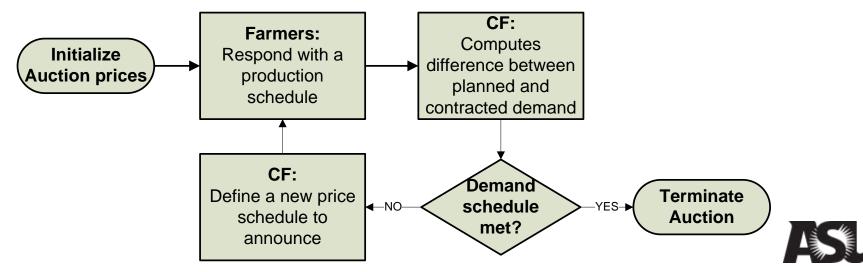
- Supply chain management is becoming increasingly important for fresh produce (Ahumada & Villalobos, 2009b; Zhang & Wilhelm, 2009)
- Must model relevant interactions, objectives and competitive behavior (A. J. Higgins et al., 2009)



Solution Approach:

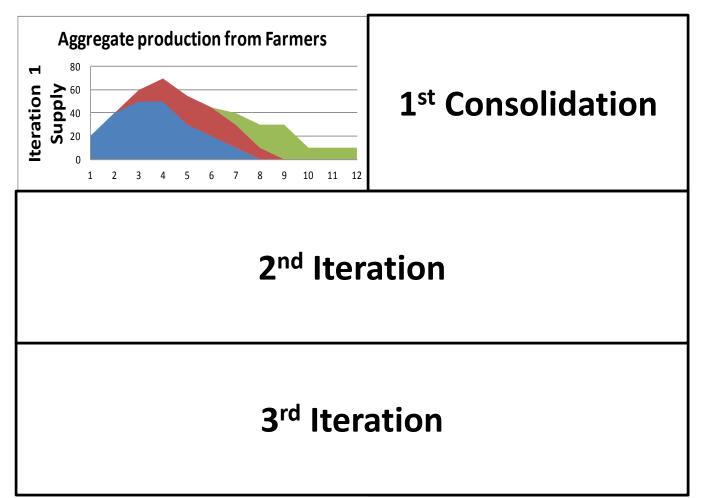
Not the traditional auction for agricultural goods

- Allocates contracts before any production has been materialized
- Auctions multiple products/units simultaneously
- Agricultural planning may be specially well suited for such a mechanism



Solution Approach:

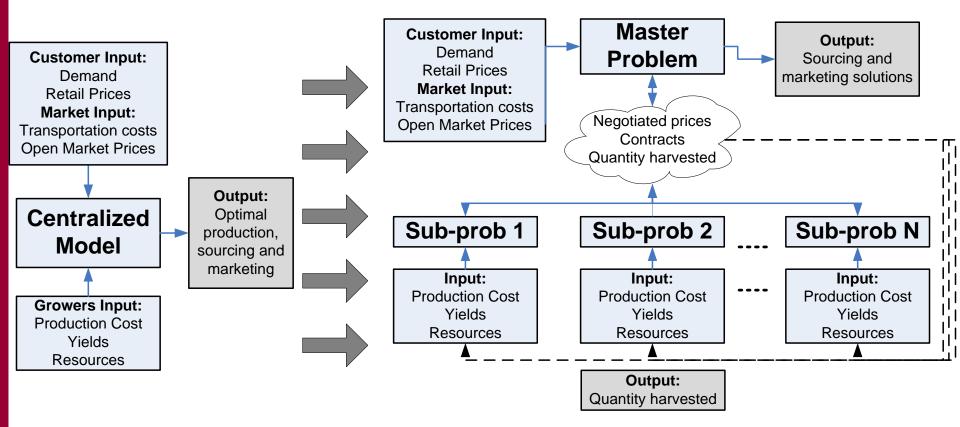
Decentralized optimization with auctions:





Models Proposed:

Centralized and decentralized models:





Mathematical Formulation:

Indexes:

$t \in$	Т	: Planning periods (weeks)
$p \in$	$P, P(j,l) \subseteq T$: Set of feasible planting weeks for crop j in location l
$h \in$	$H, H(j, l) \subseteq T$: Set of feasible harvesting weeks for crop j in location l
j ∈	J	: Potential crops to plant
$q \in$	Q	: Quality states of crops
$l \in$	L	: Locations available for planting

General Parameters (CF):

$MaxDem_{hj}$: Maximum demand of crop j at time h (Maximum open market)
$MinDem_{hj}$: Minimum demand of crop <i>j</i> at time <i>h</i> (Contracted demand)
qmin _j	: Minimum quality accepted for crop <i>j</i>
WHCap	: Total capacity of consolidation facility
Δq_j	: Change in quality for product <i>j</i> stored one week at CF



Mathematical Formulation:

General Parameters (Farmer):

- Land $_l$ Labor P_{ptj} Labor H_j MaxLab $_l$ Yield $_{phj}$ Total $_{jl}$ MaxL $_j$ MinL $_j$ QualD $_{jql}$ Δtl_l Δql_{lj}
- : Land available at location *l* (in acres)
 : Workers needed at period *t* for cultivating crop *j* planted at period *p* (Men-week/ Acre)
 - : Workers needed for harvesting crop j (Men-week/Acre)
 - : Max number of workers that can be hired in location l
 - : Expected yield of crop j at time p and harvested in week h (%/Week)
 - : Expected total production of crop *j* planted in location *l* (Cartons/Acre)
 - : Maximum allowed amount to plant of crop *j* during one week (in Acre)
 - : Minimum allowed amount to plant of crop *j* during one week (in Acre)
 - : Quality distribution q for crop j for farmer l
 - : Travel time from location *l* to facility
 - : Change in quality for product j traveling from location l to facility



Mathematical Formulation:

Cost parameters (Farmers):

Cplant _{jl}	: Cost per acre of planting and cultivating for crop <i>j</i> (exclude labor)
Charv _{jl}	: Cost per acre of harvesting for crop <i>j</i> (exclude labor)
Chire _t	: Fixed cost to hire a seasonal worker at time <i>t</i>
$Clab_t$: Variable cost to hire a seasonal worker at time <i>t</i>
Ctrans _{jl}	: Cost of transportation form location <i>l</i> to facility

Cost parameters (CF):

Cinv _j	: Inventory cost for crop <i>j</i>
Cover _j	: Cost of overage for product <i>j</i>
Cunder _j	: Cost of underage for product <i>j</i>
$Price_{hj}$: Expected price for crop <i>j</i> at time <i>h</i>



Mathematical Formulation:

Decision variables (Farmers):

Vplant _{pjl}	: Area to plant of crop j in period p at location l
$Vharv_{hjl}$: Harvest quantity of crop <i>j</i> in period <i>h</i> at location <i>l</i>
Vlab _{tl}	: Seasonal laborers employed at location <i>l</i> at time <i>t</i>
<i>VHire_{tl}</i>	: Seasonal laborers hired for location <i>l</i> at time <i>t</i>
$VFire_{tl}$: Seasonal laborers dismissed from location <i>l</i> at time <i>t</i>
Y _{jpl} (Binary)	: 1 If crop <i>j</i> is planted at period <i>p</i> at location <i>l</i> 0 otherwise
Vtrans _{hjql}	: Amount to transport from location l of crop j with quality q at time

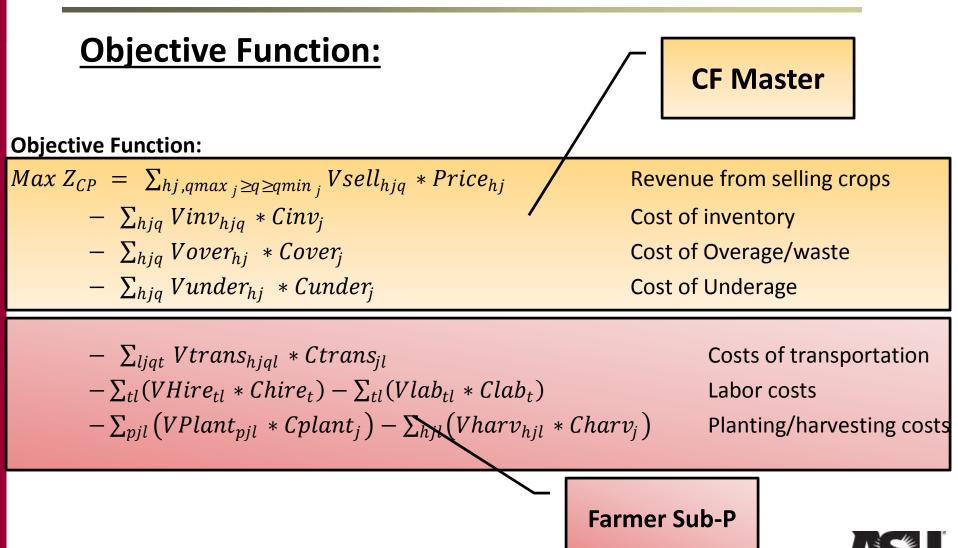
Decision variables (CF):

$Vinv_{hjq}$: Amount to store of crop j with quality q at time h
Vsell _{hjq}	: Amount of crop j to sell with quality q at time h
$Vover_{hj}$: Overage of crop <i>j</i> at time <i>h</i>
$Vunder_{hj}$: Underage of crop <i>j</i> at time <i>h</i>



h

Mathematical Formulation:



Mathematical Formulation:

Farming Constraints:

Farming Constraints:

$$\begin{array}{ll} \sum_{j} \sum_{p} Vplant_{pjl} \leq Land_{l} & \forall l \in L \\ Min_{j} * Y_{jpl} \leq Vplant_{pjl} \leq Max_{j} * Y_{jpl} & \forall j \in J, \ p \in P, l \in L \\ Vharv_{hjl} \leq \sum_{p} Vplant_{pjl} * Yield_{phj} * Total_{jl} & \forall h \in H, \ j \in J, \ l \in L \\ Vharv_{hjl} * QualD_{hjql} = Vtrans_{lj}(q - \Delta ql_{lj})(h + \Delta tl_{l}) & \forall h, j, q, l \\ \hline \mathbf{Farming Labor Constraints:} \\ Vlab_{tl} \geq \sum_{p} \sum_{j} Vplant_{pjl} * LaborP_{ptj} + \sum_{h=t} \sum_{j} Vharv_{hjl} * LaborH_{j} & \forall t \in T, l \in L \\ VHire_{tl} - VFire_{tl} = Vlab_{tl} - Vlab_{(t-1)l} & \forall t \in L \\ \end{array}$$



Mathematical Formulation:

Consolidation Facility (Master) Constraints:

Coupling Constraint:

 $\sum_{l} V trans_{hljq} = PVarr_{h,j,q} \qquad \forall j,q,h$

Inventory balance and quality tracking:

 $PVarr_{h,j,q} + Vinv_{h-1,jq+\Delta q_j} - Vsell_{hjq} - Vwaste_{hjq} = Vinv_{h,j,q} \quad \forall j,q,h$

Demand Constraints:

 $MinDem_{hj} - Vunder_{hj} \leq \sum_{qmax_j \geq q \geq qmin_j} Vsell_{hjq} \leq MaxDem_{hj} + Vover_{hj} \quad \forall \ j,h$ Warehouse Capacity Constraint:

 $\sum_{jq} Vinv_{hjq} \leq WHCap \qquad \forall h$



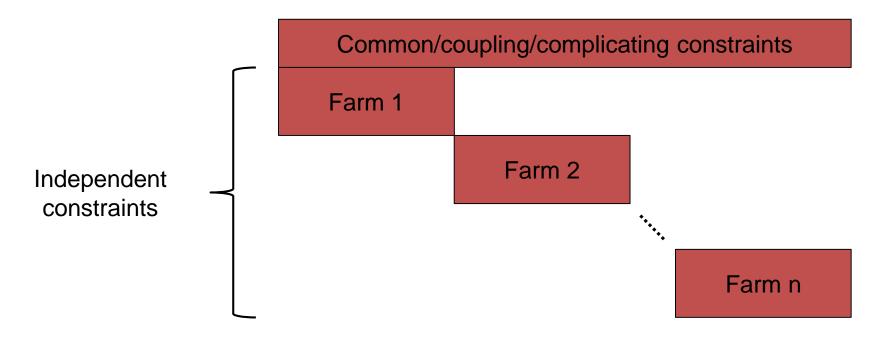
Mathematical Decomposition:

Problem has a block-angular structure:

Coupling Constraint:

 $\sum_{l} V trans_{hljq} = PVarr_{h,j,q}$

∀ j,q,*h*





Mathematical Decomposition:

Possible Decentralized Reformulations:

- Dantzig-Wolfe Decomposition
 - Dual decomposition
 - Master problem recombines local solutions
 - Less appealing to stakeholders

Subgradient optimization

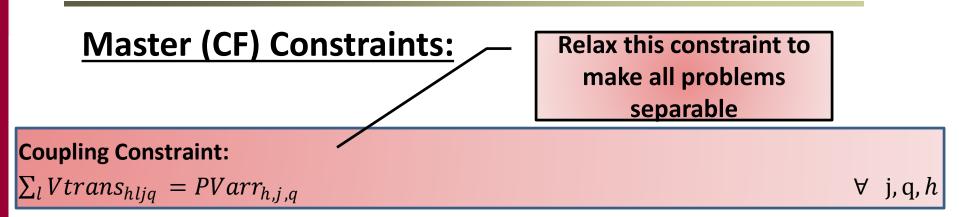
Dual decomposition

Reformulate through Sub-Gradient optimization and use vector for transfer prices

- Master problem creates a price tatonement/bidding process
- More intuitive, transparent and of apparent fairness



Mathematical Decomposition:



Inventory balance and quality tracking:

 $PVarr_{h,j,q} + Vinv_{h-1,jq+\Delta q_j} - Vsell_{hjq} - Vwaste_{hjq} = Vinv_{h,j,q}$ $\forall j,q,h$

Demand Constraints:

$$\begin{split} MinDem_{hj} - Vunder_{hj} &\leq \sum_{qmax_j \geq q \geq qmin_j} Vsell_{hjq} \leq MaxDem_{hj} + Vover_{hj} \quad \forall \ j,h \\ \textbf{Warehouse Capacity Constraint:} \\ \sum_{jq} Vinv_{hjq} \leq WHCap \qquad \qquad \forall \ h \end{split}$$



Mathematical Decomposition:

Modified Objective function:

$$\begin{aligned} Max \ Z_{SG} &= \sum_{hj,qmax_{j} \ge q \ge qmin_{j}} Vsell_{hjq} * Price_{hj} \\ &- \sum_{hjq} Vinv_{hjq} * Cinv_{j} \\ &- \sum_{hjq} Vover_{hj} * Cover_{j} \\ &- \sum_{hjq} Vunder_{hj} * Cunder_{j} \end{aligned}$$

$$\begin{aligned} &- \sum_{ljqt} Vtrans_{hjql} * Ctrans_{jl} \\ &- \sum_{tl} (VHire_{tl} * Chire_{t}) - \sum_{tl} (Vlab_{tl} * Clab_{t}) \\ &- \sum_{pjl} (VPlant_{pjl} * Cplant_{j}) - \sum_{hjl} (Vharv_{hjl} * Charv_{j}) \end{aligned}$$

Mathematical Decomposition:

Modified Objective function:

$$Max Z_{SG} = \sum_{hj,qmax_j \ge q \ge qmin_j} Vsell_{hjq} * Price_{hj} - \sum_{hjq} Vinv_{hjq} * Cinv_j - \sum_{hjq} Vover_{hj} * Cover_j - \sum_{hjq} Vunder_{hj} * Cunder_j Cost for CF - \sum_{hjq} \lambda_{hjq} (PVarr_{h,j,q})$$

$$-\sum_{ljqt} Vtrans_{hjql} * Ctrans_{jl} \\ -\sum_{tl} (VHire_{tl} * Chire_{t}) - \sum_{tl} (Vlab_{tl} * Clab_{t}) \\ -\sum_{pjl} (VPlant_{pjl} * Cplant_{j}) - \sum_{hjl} (Vharv_{hjl} * Charv_{j}) \\ +\sum_{hjq} \lambda_{hjq} (\sum_{l} Vtrans_{hljq})$$
Revenue for Farmers



Validation of the Mechanism:

Data used:

- Production data for four crops was used: (Broccoli, cauliflower, romaine lettuce and iceberg lettuce)
- Information from Yuma, AZ representing a typical farm from the region was used.
- Data used includes:
 - Production costs
 - Yields and seasonality
 - Labor costs and productivity
 - Perishability of crops
 - Historical market prices



Validation of the Mechanism:

Differences between agents (farms):

 \rightarrow

 \rightarrow

 \rightarrow

 \rightarrow

 \rightarrow

 \rightarrow

- Numerous factors can influence a farmers comparative advantage and decision processes
- Size of farm
- Soil types
- Microclimates
- Technology
- Preferences
- Access to water
- Simple know-how

bargaining power /costs
seasonality/yields/costs
seasonality/yields/costs
seasonality/yields/costs
product offerings
product offerings



Validation of the Mechanism:

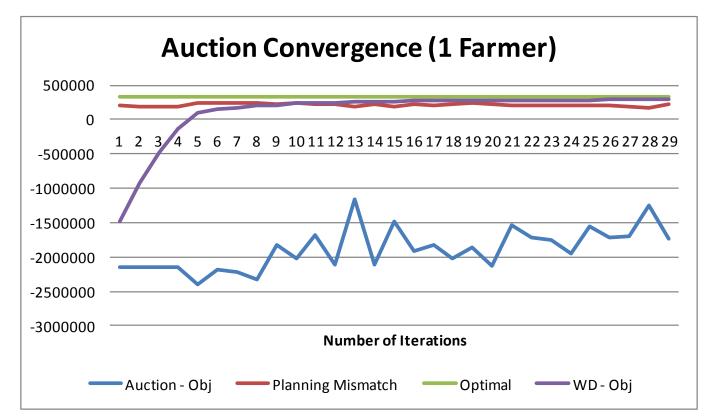
Data manipulation:

- In order to test the mechanism, the "typical farm" framework was adjusted to induce diversity among decisionmakers.
 - Land/Labor: [U~(0.5,1.5)]*(35 workers/200 acres)
 - Yield: [U~(0.75, 1.35)]* Base yield
 - Production costs: [U~(0.75, 1.35)]* Base cost
- Parameters of farmers remained hidden from one another.
 Only prices are communicated

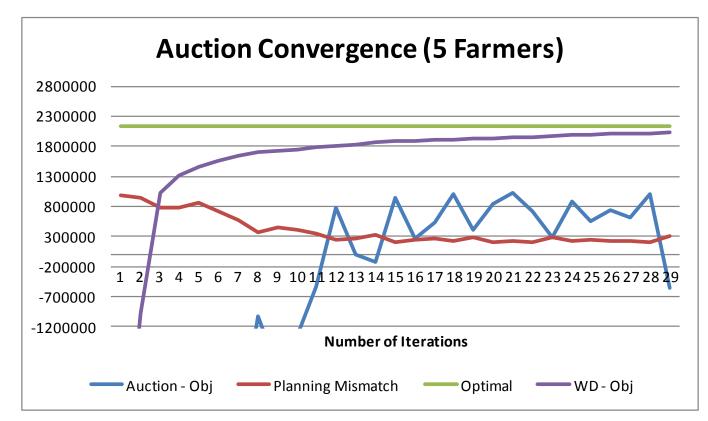


- Auction Obj: Current auction objective function value
- **Planning Mismatch:** $\sum_{hjq} (PVarr_{h,j,q} \sum_{l} Vtrans_{hljq})$
- **Optimal:** Centralized, optimal solution
- WD–Obj: Solution obtained through Wolfe Dantzig decomposition

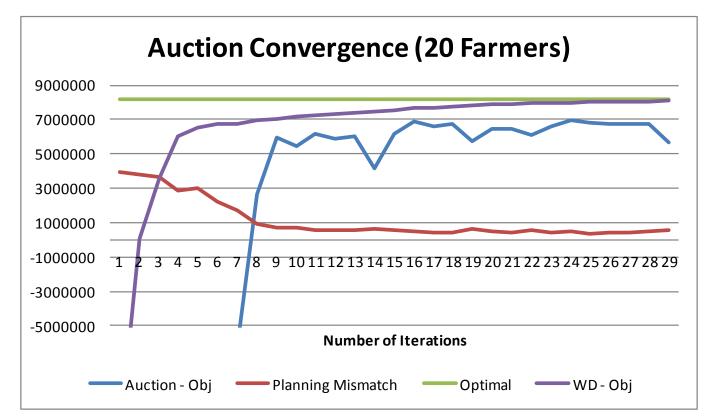




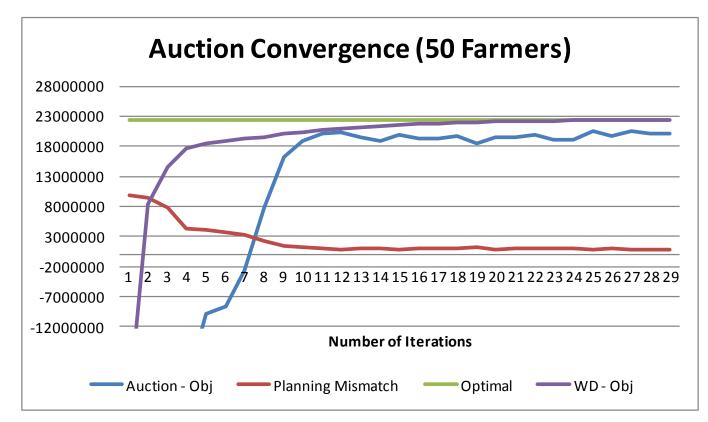




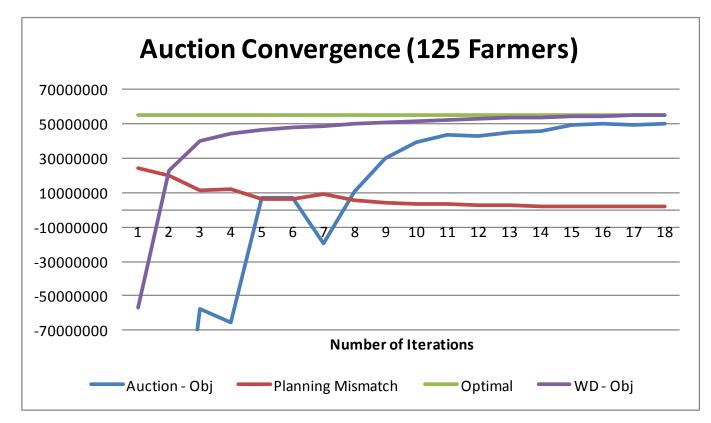








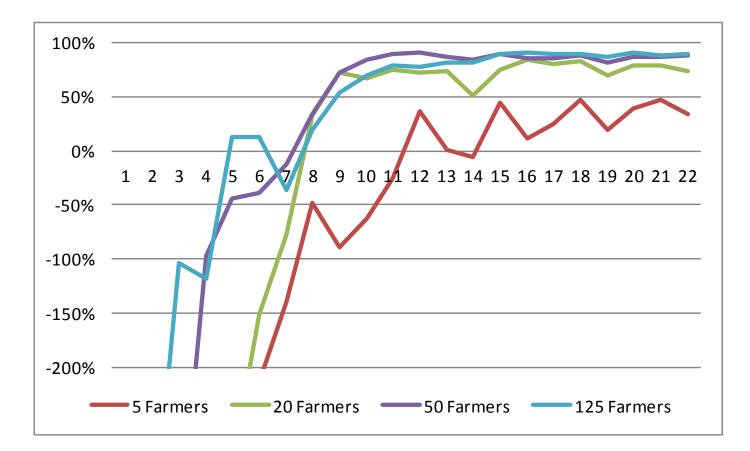






Convergence and efficiency:

Relative Optimality Gap





Convergence Summary:

- Convergence is faster at larger problem instances
- Smaller optimality gap is achieved with more players
- A reduced number of players leads to high supply elasticity
 - Few players have more control over relative supply/demand equilibrium
 - Consistent with economic theory

Number of	Number of Optimal		Be	est Auction	% Planning	%	Iteration	Iterations
participants Solution			Solution	Mismatch	Optimality	#	to 80%	
1 Farm	\$	324,269	\$	(1,161,669)	106%	-358%	13	-
5 Farms	\$	2,136,136	\$	1,020,037	25%	48%	21	-
20 Farms	\$	8,156,519	\$	6,930,982	14%	85%	24	17
50 Farms	\$	22,395,199	\$	20,601,215	8%	92%	27	10
125 Farms	\$	55,567,789	\$	50,863,300	8%	92%	20	11



Final considerations:

Benefits

- Coordination mechanism is intuitive
- Ample theoretical backing to support optimality
- Attractive for large organizations

<u>Pitfalls</u>

- Sub gradient optimization may yield infeasible solutions
- Must define penalties for demand overage/underage
- Bidders may lie to gain strategic advantage



Final Considerations:

- There should be transparency and fairness on contract allocation
- Reasonable convergence



- Agents may act strategically and attempt to influence allocation decisions
- Incentive Compatibility: No agent can be made better off by misrepresenting its information

Individual Rationality: Agents cannot be forced to

participate





Final considerations:

Further work

- Refine sub-gradient step sizes for convergence
- Reformulate a more flexible demand fulfillment
- Perform case study
- Quantify and minimize impact of strategic bidding



Solution Approach:

Analysis of efficiency:

Optimal allocation for each agent *i* (Truth)

$$Max \quad z^* = c^i x^i$$
$$st: Ax^i = b$$
$$x^i \ge 0$$

Best response (Not necessarily truth)

$$Max \quad z^{BR} = c^{i}x^{i} + \sum_{k=i}^{K-1} c^{k+1}_{(c^{k}, x^{i}, w^{i})} x^{k+1}$$
$$st: Ax^{i} = b$$
$$x^{i} \ge 0$$

BR. Includes consideration of multiple iterations "K"





- Ahumada, O., & Villalobos, J. R. (2009a). A tactical model for planning the production and distribution of fresh produce. Annals of Operations Research, 190(1), 339–358. doi:10.1007/s10479-009-0614-4
- Ahumada, O., & Villalobos, J. R. (2009b). Application of planning models in the agri-food supply chain: A review. European Journal of Operational Research, 196(1), 1–20. doi:10.1016/j.ejor.2008.02.014
- Ahumada, O., Villalobos, R. J., & Mason, A. N. (2012). Tactical planning of the production and distribution of fresh agricultural products under uncertainty. Agricultural Systems, 112, 17–26. doi:10.1016/j.agsy.2012.06.002
- Albrecht, M. (2010). Coordination Mechanisms for Supply Chain Planning. In Supply Chain Coordination Mechanisms (pp. 35–61). Springer Berlin Heidelberg. Retrieved from http://link.springer.com/chapter/10.1007/978-3-642-02833-5_3
- Ausubel, L. M., & Cramton, P. (2002). Demand Reduction and Inefficiency in Multi-Unit Auctions. Retrieved from http://drum.lib.umd.edu//handle/1903/7062
- Burer, S., Jones, P. C., & Lowe, T. J. (2008). Coordinating the supply chain in the agricultural seed industry. European Journal of Operational Research, 185(1), 354–377.



- Chen, F. (2003). Information Sharing and Supply Chain Coordination. In and A. G. de K. S.C. Graves (Ed.), Handbooks in Operations Research and Management Science (Vol. Volume 11, pp. 341–421). Elsevier. Retrieved from http://www.sciencedirect.com/science/article/pii/S0927050703110079
- Dharma, R. A., & Arkeman, Y. (2010). AN INTELLIGENT DECISION SUPPORT SYSTEM FOR HORTICULTUE. Jurnal Teknologi Industri Pertanian, 19(3). Retrieved from http://medpet.journal.ipb.ac.id/index.php/jurnaltin/article/view/1778
- Fan, M., Stallaert, J., & Whinston, A. B. (2003). Decentralized Mechanism Design for Supply Chain Organizations Using an Auction Market. Information Systems Research, 14(1), 1–22. doi:10.1287/isre.14.1.1.14763
- Frayret, J.-M., D'Amours, S., Rousseau, A., Harvey, S., & Gaudreault, J. (2008). Agent-based supply-chain planning in the forest products industry. International Journal of Flexible Manufacturing Systems, 19(4), 358–391. doi:10.1007/s10696-008-9034-z
- Higgins, A., Antony, G., Sandell, G., Davies, I., Prestwidge, D., & Andrew, B. (2004). A framework for integrating a complex harvesting and transport system for sugar production. Agricultural Systems, 82(2), 99–115. doi:10.1016/j.agsy.2003.12.004
- Higgins, A. J., Miller, C. J., Archer, A. A., Ton, T., Fletcher, C. S., & McAllister, R. R. J. (2009). Challenges of operations research practice in agricultural value chains. Journal of the Operational Research Society, 61(6), 964–973. doi:10.1057/jors.2009.57



- Karabuk, S., & Wu, S. D. (2002). Decentralizing semiconductor capacity planning via internal market coordination. IIE Transactions, 34(9), 743–759. doi:10.1023/A:1015592520287
- Kazaz, B. (2004). Production Planning Under Yield and Demand Uncertainty with Yield-Dependent Cost and Price. Manufacturing & Service Operations Management, 6(3), 209– 224.
- Kazaz, B., & Webster, S. (2011). The Impact of Yield-Dependent Trading Costs on Pricing and Production Planning Under Supply Uncertainty. Manufacturing & Service Operations Management, 13(3), 404–417. doi:10.1287/msom.1110.0335
- Manelli, A. M., & Vincent, D. R. (2006). Bundling as an optimal selling mechanism for a multiple-good monopolist. Journal of Economic Theory, 127(1), 1–35. doi:10.1016/j.jet.2005.08.007
- Manelli, A. M., & Vincent, D. R. (2007). Multidimensional mechanism design: Revenue maximization and the multiple-good monopoly. Journal of Economic Theory, 137(1), 153– 185. doi:10.1016/j.jet.2006.12.007
- McAfee, R. P., McMillan, J., & Whinston, M. D. (1989). Multiproduct Monopoly, Commodity Bundling, and Correlation of Values. The Quarterly Journal of Economics, 104(2), 371. doi:10.2307/2937852



- Mishra, D., & Veeramani, D. (2007). Vickrey–Dutch procurement auction for multiple items. European Journal of Operational Research, 180(2), 617–629. doi:10.1016/j.ejor.2006.04.020
- Myerson, R. B. (1981). Optimal Auction Design. Mathematics of Operations Research, 6(1), 58–73. doi:10.2307/3689266
- Rantala, J. (2004). Optimizing the Supply Chain Strategy of a Multi-Unit Finnish Nursery Company. Retrieved from http://citeseerx.ist.psu.edu/viewdoc/summary?doi=10.1.1.102.2847
- Schepers, H., & Van Kooten, O. (2006). Profitability of "ready-to-eat" strategies: towards model-assisted negotiation in a fresh-produce chain. Frontis, 15, 117–132.
- Vohra, R. V. (2011). Mechanism Design: A Linear Programming Approach (1st ed.). Cambridge University Press.
- Zhang, W., & Wilhelm, W. E. (2009). OR/MS decision support models for the specialty crops industry: a literature review. Annals of Operations Research, 190(1), 131–148. doi:10.1007/s10479-009-0626-0

